

# Effects of Concentration, Temperature and Hydrostatic Pressure on the Local Lattice Structure of $\text{Ni}^{2+}$ Doped $\text{Zn}(\text{BF}_4)_2 \cdot 6\text{H}_2\text{O}$ Crystal

Ming-Liang Gao<sup>a</sup>, Xiao-Yu Kuang<sup>a,b</sup>, Hui-Fang Li<sup>a</sup>, and Huai-Qian Wang<sup>a</sup>

<sup>a</sup> Institute of Atomic and Molecular Physics, Sichuan University, Chengdu 610065, China

<sup>b</sup> International Centre for Materials Physics, Academia Sinica, Shenyang 110016, China

Reprint requests to X.-Y. K.; E-mail: scu\_kuang@163.com

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A theoretical method for studying the inter-relationship between electronic and molecular structure is presented by means of complete energy matrices. As an application, the effects of temperature, concentration and hydrostatic pressure on the local structures of  $\text{Ni}^{2+}$  doped  $\text{Zn}(\text{BF}_4)_2 \cdot 6\text{H}_2\text{O}$  crystal have been studied. Our results show that the local lattice structures of  $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$  coordination complex have expansion distortions as the temperature rises. Meanwhile, we find that the local structure parameter  $\theta$  becomes smaller with the increasing concentration of  $\text{Ni}^{2+}$  ions doped in  $\text{Zn}(\text{BF}_4)_2 \cdot 6\text{H}_2\text{O}$  crystal. Furthermore, the pressure dependence of  $\theta$  and anisotropic  $g$ -factors are discussed and the relationship between zero-field splitting parameter  $D$  and  $\Delta g$  is determined.

**Key words:** Local Structure;  $\text{Zn}(\text{BF}_4)_2 \cdot 6\text{H}_2\text{O}:\text{Ni}^{2+}$  System; Complete Energy Matrices.

## 1. Introduction

With the rapid development of material science, solid material crystals doped with transition metal ions have drawn a great deal of attention in recent years [1–5]. This can be attributed to the fact that crystals with transition metal ions usually have special behaviours [6–9] which are closely related to the structure distortions. Accordingly, studying the local structures around the impurities is crucial to get a better insight into the interaction between impurity ions and host crystals and is central to realize the microscopic origin of crystal properties.

Experimentally, many methods are used to investigate the local structure of the doped systems, such as the electron nuclear double resonance (ENDOR) [10–12], the extended X-ray absorption fine structure (EXAFS) [13–15] and the electron paramagnetic resonance (EPR) [16–18]. Among them, the EPR method is considered as a powerful tool to study the microstructures and the local distortions around the impurity ions in the crystals. The reason is that the EPR spectra are sensitive to the distortion of the local structures of the transition metal ions [19,20]. The EPR spectra of  $\text{Ni}^{2+}$  ions in  $\text{Zn}(\text{BF}_4)_2 \cdot 6\text{H}_2\text{O}:\text{Ni}^{2+}$  system have been measured by many researchers [21–24]. For instance, Sano et al. have studied the tempera-

ture and concentration dependence of the EPR spectra of  $\text{Zn}(\text{BF}_4)_2 \cdot 6\text{H}_2\text{O}:\text{Ni}^{2+}$  system [21]. Krygin et al. have dealt with the pressure dependence of the EPR parameters of  $\text{Ni}^{2+}$  ions doped in  $\text{Zn}(\text{BF}_4)_2 \cdot 6\text{H}_2\text{O}$  crystal [22]. Their experimental results give important information about the ground state of the transition metal  $\text{Ni}^{2+}$  ions and form a useful starting point for understanding the inter-relationship between electronic and molecular structure of  $\text{Ni}^{2+}$  ions in the  $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$  coordination complex. So far, however, few systematical studies on the local structure parameters of  $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$  coordination complex at different concentrations, temperatures and pressures have been reported. Recently, Feng et al. have studied the effects of the temperature and pressure on the zero-field splitting (ZFS) and got the local structure parameters  $\theta = 54.80^\circ$  at 77 K and  $\theta = 54.95^\circ$  at 293 K by the complete energy matrices using a Matlab 6.5 computer program [25], but their method is based on the strong-field basis function and the local structure parameters under different concentrations have not been investigated. In the present work, the  $45 \times 45$  complete energy matrices have been constructed based on the weak-field basis function in terms of the Slater's method. The relations between the local structure and concentration, temperature and pressure are discussed systematically.

## 2. Theoretical Analysis

### 2.1. The Complete Energy Matrices for a d<sup>8</sup> Configuration Ion in a Trigonal Ligand Field

For the paramagnetic Ni<sup>2+</sup> ion in a trigonal symmetry field, the complete set of basis function includes 45 basic Slater determinants such as  $|2^+, 2^-|$ ,  $|2^+, 1^-|$ , ...,  $|2^+, -2^-|$ . Then, the wave functions  $|L, S, M_L, M_S\rangle_i$  of d<sup>8</sup> configuration in the LS-coupling scheme can be gotten based on the following expression

$$|L, S, M_L, M_S\rangle_i = \sum_j C_j \Phi_j, \quad (1)$$

where  $C_j$  is the Clebsch-Gordon coefficient and  $\Phi_j$  is one of the 45 basic Slater determinants.

The perturbation Hamiltonian for a d<sup>8</sup> configuration ion in a trigonal ligand-field can be expressed as [25]

$$\begin{aligned} \hat{H} &= \hat{H}_{ee} + \hat{H}_{SO} + \hat{H}_{LF} + \hat{H}_{Zeeman} \\ &= \sum_{i < j} \frac{e^2}{r_{ij}} + \zeta \sum_i l_i s_i + \sum_i V_i \\ &\quad + \sum_i \mu_B (k \vec{l}_i + g_e \vec{s}_i) \cdot \vec{H}, \end{aligned} \quad (2)$$

where the first term is the electron-electron interaction, the second term is the spin-orbit coupling interaction, the third term denotes the ligand-field interaction, and the last term represents the Zeeman interaction.  $\zeta$  and  $k$  are the spin-orbit coupling coefficient and the orbital reduction factor, respectively.  $V_i$  is the potential function which can be expressed as

$$\begin{aligned} V_i &= \gamma_{00} Z_{00} + \gamma_{20} r_i^2 Z_{20}(\theta_i, \varphi_i) + \gamma_{40} r_i^4 Z_{40}(\theta_i, \varphi_i) \\ &\quad + \gamma_{43}^c r_i^4 Z_{43}^c(\theta_i, \varphi_i) + \gamma_{43}^s r_i^4 Z_{43}^s(\theta_i, \varphi_i), \end{aligned} \quad (3)$$

where  $r_i$ ,  $\theta_i$  and  $\varphi_i$  are the spherical coordinates of the  $i$ -th electron.  $Z_{lm}$ ,  $Z_{lm}^c$  and  $Z_{lm}^s$  are the real spherical harmonics.  $\gamma_{00}$ ,  $\gamma_{lm}^c$  and  $\gamma_{lm}^s$  are associated with the local structure around a d<sup>8</sup> configuration ion by the relations

$$\begin{aligned} \gamma_{00} &= -\frac{4\pi}{2l+1} \sum_{\tau=1}^n \frac{eq_{\tau}}{R_{\tau}^{l+1}} Z_{l0}(\theta_{\tau}, \varphi_{\tau}), \\ \gamma_{lm}^c &= -\frac{4\pi}{2l+1} \sum_{\tau=1}^n \frac{eq_{\tau}}{R_{\tau}^{l+1}} Z_{lm}^c(\theta_{\tau}, \varphi_{\tau}), \\ \gamma_{lm}^s &= -\frac{4\pi}{2l+1} \sum_{\tau=1}^n \frac{eq_{\tau}}{R_{\tau}^{l+1}} Z_{lm}^s(\theta_{\tau}, \varphi_{\tau}), \end{aligned} \quad (4)$$

where  $\theta_{\tau}$  and  $\varphi_{\tau}$  are angular coordinates of the ligand,  $\tau$  and  $q_{\tau}$  represent the  $\tau$ -th ligand ion and its effective charge, respectively, and  $R_{\tau}$  denotes the metal-ligand distance.

The  $45 \times 45$  complete energy matrices for a d<sup>8</sup> configuration ion corresponding to the perturbation Hamiltonian have been constructed by using the Slater wave function method and the calculating procedure. The matrix elements can be expressed as the functions of the Racah parameters  $B$ ,  $C$ , the spin-orbit coupling coefficient  $\zeta$ , the orbital reduction factor  $k$ , and the ligand-field parameters  $B_{20}$ ,  $B_{40}$ ,  $B_{43}^c$  and  $B_{43}^s$ . For the Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O:Ni<sup>2+</sup> system, the Ni<sup>2+</sup> ion is surrounded by six H<sub>2</sub>O molecules and the local structure symmetry belongs to the  $D_{3d}$  symmetry [22]. In general, the z-axis is chosen along the three fold axis and the x-axis is chosen to be consistent with the projection of one of the impurity-ligand bond in x-y plane. Then, the ligand-field parameter  $B_{43}^s$  will vanish, and  $B_{20}$ ,  $B_{40}$ ,  $B_{43}^c$  can be expressed as [26]

$$\begin{aligned} B_{20} &= \frac{1}{2} \sum_{\tau} G_2(\tau) (3 \cos^2 \theta_{\tau} - 1), \\ B_{40} &= \frac{1}{8} \sum_{\tau} G_4(\tau) (35 \cos^4 \theta_{\tau} - 30 \cos^2 \theta_{\tau} + 3), \\ B_{43}^c &= \frac{\sqrt{35}}{4} \sum_{\tau} G_4(\tau) \sin^3 \theta_{\tau} \cos \theta_{\tau}. \end{aligned} \quad (5)$$

According to the Van Vleck approximation [27],  $G_2(\tau)$  and  $G_4(\tau)$  can be expressed as

$$\begin{aligned} G_2(\tau) &= -eq_{\tau} \frac{\langle r^2 \rangle}{R_{\tau}^3} = \frac{A_2}{R_{\tau}^3}, \\ G_4(\tau) &= -eq_{\tau} \frac{\langle r^4 \rangle}{R_{\tau}^5} = \frac{A_4}{R_{\tau}^5}, \end{aligned} \quad (6)$$

where

$$A_2 = -eq_{\tau} \langle r^2 \rangle, \quad A_4 = -eq_{\tau} \langle r^4 \rangle, \quad \frac{A_2}{A_4} = \frac{\langle r^2 \rangle}{\langle r^4 \rangle}. \quad (7)$$

The ratio  $\langle r^2 \rangle / \langle r^4 \rangle = 0.141029$  is derived from the empirical radial wave function of Ni<sup>2+</sup> in complexes [28].  $A_4$  is almost a constant for [Ni(H<sub>2</sub>O)<sub>6</sub>]<sup>2+</sup> coordination complex and its value can be obtained from the corresponding optical spectra. Then,  $A_2$  can be determined by (7). Although no optical spectra of Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O:Ni<sup>2+</sup> system has been observed, it is reasonable to apply the optical spectra of NiSiF<sub>6</sub> · 6H<sub>2</sub>O in calculation since they have the similar crystal structure and the same type of ligand. Therefore, we obtain

$A_4 = 20.9$  a. u. from the optical spectra and the local structure of the NiSiF<sub>6</sub> · 6H<sub>2</sub>O [29, 30]. The advantage of determining the value of  $A_4$  is to reduce the number of adjustable parameters and make the choosing of parameters more reasonable. Thus, the ligand-field parameters  $B_{20}$ ,  $B_{40}$ ,  $B_{43}^c$  are only the functions of distortion parameters  $R_\tau$  and  $\theta_\tau$  which are strongly depended on the external factors such as temperature, concentration and pressure.

## 2.2. EPR Parameters for a $d^8$ Configuration Ion

EPR spectra for a  $d^8$  configuration ion in a trigonal ligand-field can be analyzed by the spin Hamiltonian [31]

$$\hat{H}_S = \mu_B g_{\parallel} H_z S_z + \mu_B g_{\perp} (H_x S_x + H_y S_y) + D \left[ S_z^2 - \frac{1}{3} S(S+1) \right], \quad (8)$$

where  $D$  is the ZFS parameter.  $H_x$ ,  $H_y$  and  $H_z$  represent the components of an external magnetic field along the x, y and z-axes, respectively. It is well known that the ground state  $^3A_2$  is split into the singlet  $|0\rangle$  and the doublet  $|\pm 1\rangle$  in the trigonal ligand-field in the absence of an external magnetic field. From the spin Hamiltonian, the splitting energy levels in the ground state  $^3A_2$  for a zero magnetic field can be given as follows

$$\begin{aligned} E(M_s = 0) &= -\frac{2}{3}D, \\ E(M_s = \pm 1) &= \frac{1}{3}D. \end{aligned} \quad (9)$$

Then, the ZFS energy  $\Delta E$  in the ground state  $^3A_2$  can be explicitly expressed as a function of the ZFS parameter  $D$

$$\Delta E = E(M_s = \pm 1) - E(M_s = 0) = D. \quad (10)$$

By diagonalizing the  $45 \times 45$  complete energy matrices, we can obtain all the crystal-field energy levels in the trigonal ligand-field with zero-magnetic field.

When considering the external magnetic field effect, the ground state  $^3A_2$  will be further split by the actual Zeeman interaction

$$\hat{H}_{\text{Zeeman}} = \sum_i \mu_B (k \vec{l}_i + g_e \vec{s}_i) \cdot \vec{H}, \quad (11)$$

where  $k$  is the orbital reduction factor describing the covalence and overlap effects on the orbital angular

momentum.  $g_e$  is the  $g$ -factor of the free electron ( $g_e = 2.0023$ ). The energy levels of the ground state  $^3A_2$  with a magnetic field including the parallel and perpendicular component of Zeeman term are given as follows.

For the magnetic field parallel to the  $C_3$  axis, the splitting energy levels of the ground state can be expressed as

$$\begin{aligned} E_1 &= -\frac{2}{3}D, \\ E_2 &= \frac{1}{3}D - g_{\parallel} \mu_B H_z, \\ E_3 &= \frac{1}{3}D + g_{\parallel} \mu_B H_z. \end{aligned} \quad (12)$$

For the magnetic field perpendicular to the  $C_3$  axis, the splitting energy levels of the ground state can be expressed as

$$\begin{aligned} E_1 &= \frac{1}{3}D, \\ E_2 &= -\frac{1}{6}D + \frac{1}{2} \sqrt{D^2 + 4g_{\perp}^2 \mu_B^2 H_{\perp}^2}, \\ E_3 &= -\frac{1}{6}D - \frac{1}{2} \sqrt{D^2 + 4g_{\perp}^2 \mu_B^2 H_{\perp}^2}. \end{aligned} \quad (13)$$

The anisotropic  $g$ -factors ( $g_{\parallel}$ ,  $g_{\perp}$ ) and ZFS parameter  $D$  for a  $d^8$  configuration ion in a trigonal ligand-field can be deduced from (12), (13) and the eigenvalues of the  $45 \times 45$  complete energy matrices.

## 3. Calculation and Discussion

### 3.1. Calculation of the Local Structures of $[\text{Ni}(\text{H}_2\text{O})_6]^{2+}$ Coordination Complex at Different Temperatures and Concentrations

Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O crystal has a pseudo hexagonal structure. The Zn<sup>2+</sup> ion is surrounded by six H<sub>2</sub>O molecules, which make up an octahedral structure slightly distorted along the  $C_3$  axis. The  $[\text{Zn}(\text{H}_2\text{O})_6]^{2+}$  octahedron site is at the center of another flattened octahedron formed by six [BF<sub>4</sub>]<sup>−</sup> tetrahedrons, which also forms an octahedral structure [21]. When doped into Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O crystal, the Ni<sup>2+</sup> ions will substitute the Zn<sup>2+</sup> ions at the octahedral sites and the point symmetry of the H<sub>2</sub>O octahedron surrounding the Ni<sup>2+</sup> ion is approximately  $D_{3d}$ . The local structure around the Ni<sup>2+</sup> ion can be described by two parameters  $R$  and  $\theta$ , which denote the Ni<sup>2+</sup>-H<sub>2</sub>O distance and the

Table 1. The EPR parameters  $D$ ,  $g_{\parallel}$  and  $g_{\perp}$  as a function of the parameters  $R$  and  $\theta$  at 4.2 K, 77 K and room temperature (RT for short) when 1% Ni<sup>2+</sup> ions doped in Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O crystal.

$T$ (K)	$R$ (Å)	$\theta$ (°)	$g_{\parallel}$	$g_{\perp}$	$-D$ (cm <sup>-1</sup> )
4.2 Calc.	2.032	54.779	2.2301	2.2291	0.135
Obsd. <sup>a</sup>			2.23±0.002	2.19±0.002	0.1350±0.0004
77 Calc.	2.033	54.796	2.2309	2.2295	0.19067
Obsd. <sup>a</sup>			2.23±0.005	2.23±0.005	0.1908±0.0004
RT Calc.	2.047	54.928	2.2351	2.2305	0.63147
Obsd. <sup>a</sup>			2.22±0.005	2.22±0.005	0.6314±0.0030

<sup>a</sup> Spectra data obtained from [22].

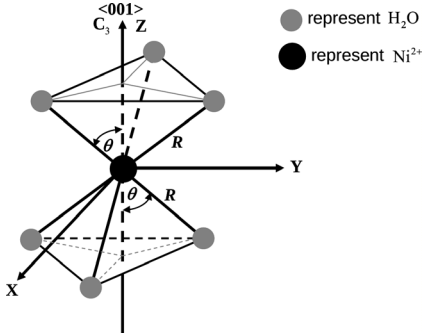


Fig. 1. Local structure of Ni<sup>2+</sup> ion in the Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O:Ni<sup>2+</sup> system.

angle between Ni<sup>2+</sup>-H<sub>2</sub>O bond and C<sub>3</sub> axis, as shown in Figure 1.

According to Curie *et al.*'s covalence theory [32], the Racah parameters  $B$ ,  $C$  and spin-orbit coupling coefficient  $\zeta$  can be reasonably expressed as

$$B = N^4 B_0, \quad C = N^4 C_0, \quad \zeta = N^2 \zeta_0, \quad (14)$$

where  $N$  is the average covalence factor,  $B_0 = 1084 \text{ cm}^{-1}$ ,  $C_0 = 4831 \text{ cm}^{-1}$ ,  $\zeta_0 = 649 \text{ cm}^{-1}$  are given for free Ni<sup>2+</sup> ion [33]. The covalence factor  $N = 0.965$  can be obtained from the optical spectra of NiSiF<sub>6</sub> · 6H<sub>2</sub>O crystal [29]. Then,  $k \approx N^2$  can also be obtained. The EPR parameters for 4.2 K, 77 K and room temperature when 1% Ni<sup>2+</sup> impurities doped in Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O crystal have been measured by Krygin *et al.* [22]. By diagonalizing the complete energy matrices, the local structure parameters  $R$  and  $\theta$  of [Ni(H<sub>2</sub>O)<sub>6</sub>]<sup>2+</sup> coordination complex at 4.2 K, 77 K and room temperature when 1% Ni<sup>2+</sup> doped in Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O crystal can be determined by simulating the optical and corresponding EPR spectra. Quantitative calculated results are listed in Tables 1 and 2. As shown in Tables 1 and 2, the calculated values agree well with the experimental values. Table 1 depicts that the lo-

Table 2. The observed and calculated optical spectra of [Ni(H<sub>2</sub>O)<sub>6</sub>]<sup>2+</sup> in NiSiF<sub>6</sub> · 6H<sub>2</sub>O crystal at 4.2 K, 77 K and room temperature (all units in cm<sup>-1</sup>).

Transition	4.2 K		77 K		Room temp.	
	Obsd. <sup>a</sup>	Calc.	Obsd. <sup>a</sup>	Calc.	Obsd. <sup>a</sup>	Calc.
<sup>3</sup> A <sub>2</sub> (F) → <sup>3</sup> T <sub>2</sub> (F)	9150	9150	9120	8800	9124	8794
		9161		9140		8843
<sup>3</sup> T <sub>1</sub> (F)	15400	15129	15290	15093	14800	14618
		15149		15122		14707
<sup>1</sup> E(D)		15363		15362		15345
<sup>1</sup> T <sub>2</sub> (D)		24083		24054		23677
		24104		24082		23769
<sup>1</sup> A(G)	24450	24763		24755		24643
<sup>3</sup> T <sub>1</sub> (P)	26100	26401	26000	26351		25774
		26456		26429		26014
<sup>1</sup> T <sub>1</sub> (G)		28809	29070	28783	28820	28453
		28820		28799		28502

<sup>a</sup> Spectra data obtained from [29].

Table 3. The EPR parameters  $D$ ,  $g_{\parallel}$  and  $g_{\perp}$  as a function of the parameters  $R$  and  $\theta$  at 4.2 K, 77 K and room temperature (RT for short) when 1.5% (2.7% for 4.2 K) Ni<sup>2+</sup> ions doped in Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O crystal.

$T$ (K)	$R$ (Å)	$\theta$ (°)	$g_{\parallel}$	$g_{\perp}$	$-D$ (cm <sup>-1</sup> )
4.2 Calc.	2.032	54.777	2.2378	2.2368	0.12905
Obsd. <sup>a</sup>			2.229±0.006	2.261±0.025	0.1291±0.0008
77 Calc.	2.033	54.796	2.2387	2.2372	0.18973
Obsd. <sup>a</sup>			2.27±0.006	2.263±0.028	0.1898±0.0009
RT Calc.	2.047	54.925	2.2486	2.2438	0.62018
Obsd. <sup>a</sup>			2.24±0.012	2.25±0.012	0.620±0.0040

<sup>a</sup> Spectra data obtained from [21].

Table 4. The EPR parameters  $D$ ,  $g_{\parallel}$  and  $g_{\perp}$  as a function of the parameters  $R$  and  $\theta$  at 4.2 K, 77 K and room temperature (RT for short) when 100% Ni<sup>2+</sup> ions doped in Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O crystal.

$T$ (K)	$R$ (Å)	$\theta$ (°)	$g_{\parallel}$	$g_{\perp}$	$-D$ (cm <sup>-1</sup> )
4.2 Calc.	2.032	54.775	2.2507	2.2497	0.124
Obsd. <sup>a</sup>			2.27±0.04		0.1240±0.0050
77 Calc.	2.033	54.79	2.2515	2.2501	0.1703
Obsd. <sup>a</sup>			2.254±0.020	2.366±0.020	0.1703±0.0010
RT Calc.	2.047	54.899	2.2616	2.2572	0.5371
Obsd. <sup>a</sup>			2.311±0.025	2.226±0.025	0.537±0.0040

<sup>a</sup> Spectra data obtained from [21].

cal structure around the octahedral Ni<sup>2+</sup> ion has an expansion tendency with increasing temperature. It can be seen that  $R = 2.032 \text{ Å}$  for 4.2 K and  $R = 2.033 \text{ Å}$  for 77 K, suggesting that  $R$  is almost changeless in the low temperature range.

The EPR parameters for different temperatures when 1.5% and 100% Ni<sup>2+</sup> impurities doped in Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O crystal have been studied by Sano

et al. [21]. As mentioned by many authors [34–36], the ZFS parameter  $D$  strongly depends on  $\theta$ . Therefore, in order to study the behaviour of  $\theta$  under different concentrations,  $R$  is fixed for the certain temperature. Then, the local angle under different concentrations can be obtained by simulating EPR spectra and the calculated results are shown in Tables 3 and 4, respectively. Comparing with Tables 1, 3 and 4, we can see that  $\theta$  decreases when the Ni<sup>2+</sup> molar concentration increases from 1% to 100%. This may be ascribed to that the ionic radius of Ni<sup>2+</sup> is smaller than that of Zn<sup>2+</sup>, and when Ni<sup>2+</sup> ions replace the Zn<sup>2+</sup> ions in Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O crystal, the Ni<sup>2+</sup> ions will pull the H<sub>2</sub>O ligands inwards.

### 3.2. Calculation of the Local Structures of [Ni(H<sub>2</sub>O)<sub>6</sub>]<sup>2+</sup> Coordination Complex at Different Pressures

The observed hydrostatic pressure dependence of  $D$  at 77 K, i.e.  $D = (-0.196 + 0.06P) \text{ cm}^{-1}$  and the

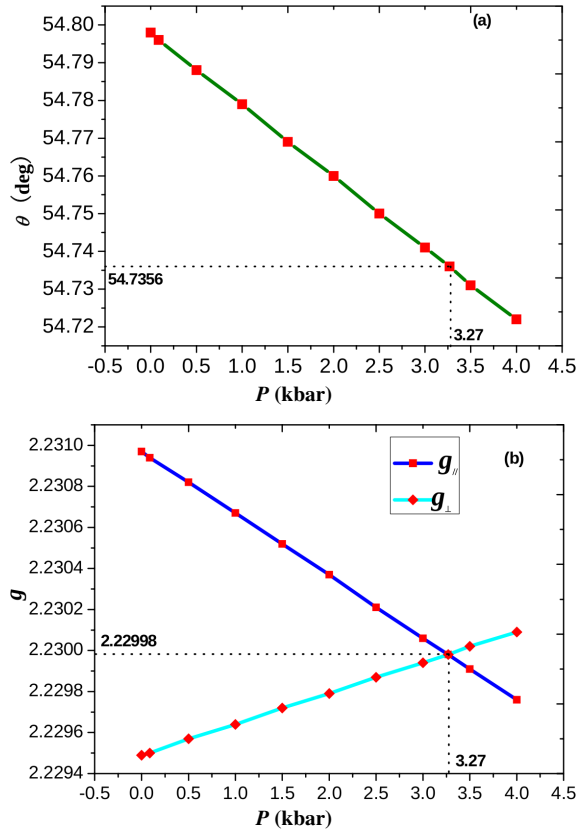


Fig. 2. Pressure dependence of (a) local structure parameter  $\theta$  and (b) g-factors ( $g_{||}$  and  $g_{\perp}$ ).

Table 5. The EPR parameters  $D$ ,  $g_{||}$  and  $g_{\perp}$  in the pressure range  $0 \text{ kbar} \leq P \leq 4 \text{ kbar}$  at 77 K for Ni<sup>2+</sup> doped Zn(BF<sub>4</sub>)<sub>2</sub> · 6H<sub>2</sub>O crystal as a function of  $\theta$ . (The values of  $D_{\text{Expt.}}$  and  $D_p$  are obtained from the experimental formula  $D = (-0.196 + 0.06P) \text{ cm}^{-1}$  [22] and from the  $45 \times 45$  complete energy matrices, respectively.)

$P$ (kbar)	$-D_{\text{Expt.}}$ (cm <sup>-1</sup> )	$g_{  }$	$g_{\perp}$	$\Delta g$	$\theta$ (°)	$-D_p$ (cm <sup>-1</sup> )
0	0.196	2.23097	2.22949	0.00148	54.798	0.196
0.087	0.1908	2.23094	2.2295	0.00144	54.796	0.1907
0.5	0.166	2.23082	2.22957	0.00125	54.788	0.1659
1.0	0.136	2.23067	2.22964	0.00103	54.779	0.1361
1.5	0.106	2.23052	2.22972	0.00080	54.769	0.1060
2.0	0.076	2.23037	2.22980	0.00057	54.76	0.0761
2.5	0.046	2.23021	2.22987	0.00034	54.75	0.0459
3.0	0.016	2.23006	2.22994	0.00012	54.741	0.0160
3.27	0	2.22998	2.22998	0	54.7356	0
3.5	-0.014	2.22991	2.23002	-0.00011	54.731	-0.0139
4.0	-0.044	2.22976	2.23009	-0.00033	54.722	-0.0441

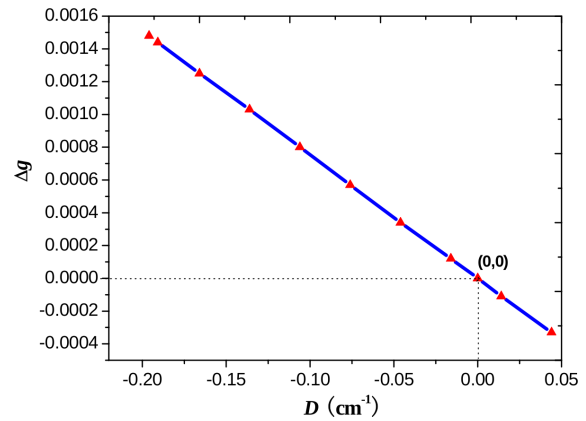


Fig. 3. The relationship between ZFS parameter  $D$  and  $\Delta g$ .

value  $D = (-0.1908 \pm 0.0004) \text{ cm}^{-1}$  have been obtained by Krygin et al. [22], from which we can get  $P \approx 0.089 \text{ kbar}$ . The local structure parameters  $R = 2.033 \text{ \AA}$  and  $\theta = 54.796^\circ$  at  $P \approx 0.089 \text{ kbar}$  are given in Tables 1 and 3. As previously mentioned,  $R$  is almost changeless in the low temperature range. Therefore, in order to discern the relationship between  $\theta$  and  $P$ ,  $R = 2.033 \text{ \AA}$  is considered as a constant. The relationship between the EPR parameters and the local structure parameter  $\theta$  in the pressure range  $0 \text{ kbar} \leq P \leq 4 \text{ kbar}$  at 77 K is shown in Table 5. The pressure dependence of the local structure parameter  $\theta$  and anisotropic g-factors ( $g_{||}$  and  $g_{\perp}$ ) are depicted in Figure 2 and the relationship between  $D$  and  $\Delta g$  ( $g_{||} - g_{\perp}$ ) is shown in Figure 3.

As depicted in Figure 2,  $\theta$  diminishes along with the increasing pressure and the relation between them

is approximately linear. Moreover, Figure 2 indicates that  $g_{\parallel}$  decreases while  $g_{\perp}$  increases with increasing pressure. Figure 3 shows that  $D$  and  $\Delta g$  reverse sign in a correlated way, i. e. for  $D < 0$ ,  $\Delta g > 0$ , whereas for  $D > 0$ ,  $\Delta g < 0$ . It's worth pointing that when the pressure reaches to 3.27 kbar,  $D = 0$ s and  $g_{\parallel} = g_{\perp} = 2.22998$ . Meanwhile, the angle becomes  $54.7356^\circ$ , which is the angle when the ligand octahedron is a cubic symmetry.

#### 4. Conclusion

The local structures for  $\text{Ni}^{2+}$  ions in  $\text{Zn}(\text{BF}_4)_2 \cdot 6\text{H}_2\text{O}:\text{Ni}^{2+}$  system at different temperatures (4.2 K, 77 K, and room temperature), molar concentrations (1%, 1.5%, and 100%), and pressures ( $0 \text{ kbar} \leq P \leq 4 \text{ kbar}$ ) are determined by diagonalizing the  $45 \times 45$  complete energy matrices. From the above studies, we have the following conclusions:

(i) The local structures around the octahedral  $\text{Ni}^{2+}$  ion have expansion distortions with the increasing temperature.

(ii) The calculated results show that  $\theta$  becomes smaller with increasing concentration of  $\text{Ni}^{2+}$  ions doped in  $\text{Zn}(\text{BF}_4)_2 \cdot 6\text{H}_2\text{O}$  crystal. We attribute it to that the ionic radius of  $\text{Ni}^{2+}$  is smaller than that of  $\text{Zn}^{2+}$  and the  $\text{Ni}^{2+}$  ion will pull the  $\text{H}_2\text{O}$  ligands inwards.

(iii) The structure parameter  $\theta$  will decrease as the pressure increases and the relation between them are approximately linear. Meanwhile, the results show that  $g_{\parallel}$  decreases while  $g_{\perp}$  increases with increasing pressure and  $D$  and  $\Delta g$  reverse sign in a correlated way, i. e. for  $D < 0$ ,  $\Delta g > 0$ , whereas for  $D > 0$ ,  $\Delta g < 0$ . Of course, careful experimental investigations, especially the optical spectra experiments, are required in order to clarify the local structure for  $\text{Ni}^{2+}$  ions in  $\text{Zn}(\text{BF}_4)_2 \cdot 6\text{H}_2\text{O}:\text{Ni}^{2+}$  system in detail.

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