

# Novel Asymptotic Soliton Waves for the Nonlinear Schrödinger Equation with Varying Gain/Loss and Frequency Chirping

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This paper analysis spatial asymptotic waves propagation in nonuniform optical fiber. It finds an appropriate transformation such that the nonlinear variable-coefficient Schrödinger equation transform into the nonlinear Schrödinger equation with varying gain/loss and frequency chirping. It obtains solitonlike and periodic self-similar asymptotic waves by using the transformation. We analyze the evolution properties of some novel self-similar solutions. In addition, the nature of our self-similar asymptotic wave hints to the possibility of designing optical amplifier and focusing of spatial waves to overcome inevitable energy losses while performing in the optical nonlinear media.

*Key words:* Self-Similar Asymptotic Wave; Nonlinear Schrödinger Equation; Varying Gain/Loss; Frequency Chirping.

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